

Migrations, Long-run Fiscal Sustainability and Economic Unions

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Introduction: labor mobility in currency unions

- Short run (Mundell [1961]):
 - mitigates the adverse impact of local shocks
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- Short run (Mundell [1961]):
 - mitigates the adverse impact of local shocks
 - compensates for the absence of local monetary authorities
- Long run (currency union → economic union):
 - challenges social security systems in sending countries
 - increases public debt burden per capita
 - rises the old-age dependency ratio
 - decreases the marginal productivity of capital
 - the opposite holds for receiving countries

- Issues covered in our work:
 - labor mobility and optimal fiscal policy
 - economic impact of migrations at the union-wide level
- Gap in the literature: no theoretical works on the long-run fiscal effects of labor mobility in currency unions
- Related papers: [▶ Literature](#)

- Starting point - the model by Song, Storesletten and Zilibotti [2012]:
 - continuum of countries
 - two overlapping generations: young and old
 - production factors: capital and labor
 - fiscal rules set by governments
 - time-consistent fiscal policy

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- Our extensions:
 - cross-country labor mobility
 - country-level productivity shocks
 - debt renegotiation

Model: demography and migration

- Number of old agents at the beginning of the period: n^o
- Every old agent delivers one young agent
- Survival rate: $\sigma \in (0, 1)$
- Only young agents can migrate (a once and for all decision)

Model: agent preferences

- Maximization problem:

$$U^y = \max_{c^y, c^{o'}, a'} \log c^y + \sigma \cdot \left[\log c^{o'} + \theta^o \cdot \mathbb{E}(\log g') \right]$$

subject to:

$$c^y + a' = (1 - \tau) \cdot w$$

$$c^{o'} = R^h \cdot a'$$

- Optimal policy rule:

$$c^y(\tau, w) = \frac{1}{1 + \sigma} \cdot (1 - \tau) \cdot w$$

Model: migration process

- Two stages of the individual migrations process:
 1. Assignment: every young agent draws a migration opportunity \hat{c} from the distribution with c.d.f. $\Phi \circ F$ (with $\Phi' > 0$, $\Phi'' > 0$)
 2. Decision: migration decision is positive with probability $\Psi\left(\frac{\hat{c}-c}{\bar{c}}\right)$ where $\Psi' > 0$

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- Number of emigrants: E
- Number of immigrants: I
- Number of young agents who live in a given country (produce and consume):

$$n^y(n^o, U^y, F) = n^o + I(n^o, U^y, F) - E(n^o, U^y, F)$$

- Formulas for E and I : [▶ details](#)
- Gross migration rate:

$$\eta \equiv \frac{n^y}{n^o}$$

Model: production

- Country-level productivity: y
- Debt renegotiation: $d \in [0, 1]$
- Aggregate productivity: $\chi(d) \cdot y$ with $\chi' < 0$ and $\chi'' < 0$

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- Firm's maximization problem:

$$\max_{K, N} \chi(d) y \cdot K^\alpha N^{1-\alpha} - wN - R^f K$$

- Capital: perfect cross-border mobility, depreciates at rate 100% after one period
- Local labor market clearing: $n^y = N$

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- Country-level wage:

$$w = (1 - \alpha) \left(\frac{\alpha}{R^f} \right)^{\frac{\alpha}{1-\alpha}} \cdot (\chi(d) \cdot y)^{\frac{1}{1-\alpha}}$$

Model: government

Government problem:

$$\max_{\tau, g, b', d} \{\alpha^y \cdot U^y + \alpha^o \cdot U^o\}$$

where

$$U^y = \log c^y(\tau, w(d, y)) + \sigma \cdot \log c^{o'}(\tau, w(d, y)) + \sigma \cdot \theta^o \cdot \mathbb{E} \log \Gamma(b', y')$$

$$U^o = \log c^o(\tau_{-1}, w_{-1}) + \theta^o \cdot \log(g)$$

α^y and α^o are Pareto weights, proportional to population size

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s.t.

$$\underbrace{\sigma \cdot g}_{\text{public spending}} + \underbrace{(1-d) \cdot (-b)}_{\text{outstanding debt}} = \underbrace{\tau \cdot w(d, y) \cdot \eta(U^y)}_{\text{tax revenues}} + \underbrace{q(b', y) \cdot (-b') \cdot \eta(U^y)}_{\text{issued debt}}$$

Model: competitive financial intermediaries and equilibrium

- Trade all types of assets
- Risk neutral, exogenous interest rate R
- Maximization problem details: [▶ details](#)
- Consistency conditions: [▶ details](#)
- MPE definition: [▶ details](#)

Model: migration and optimal fiscal policy

1. Redistribution from old to young (governments compete for labor force!)

- from public spending to private consumption

$$g = \underbrace{\theta^o \cdot c^y}_{g \text{ when no migration}} - \underbrace{\frac{\eta'}{\eta} \cdot \theta^o \cdot [\tau \cdot w - q \cdot b']}_{\text{fiscal benefits from labor inflows}}$$

- analogously, government redistributes from public spending today to public spending tomorrow by decreasing the level of debt

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2. Optimal debt renegotiation:

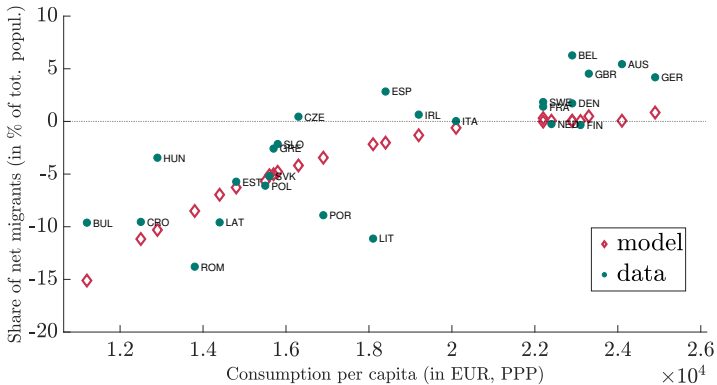
$$d = \operatorname{argmax} (1 - d) \cdot b + w(d, y) \cdot \eta(U^y)$$

- it is less costly to default for sending countries and more costly to default for receiving countries

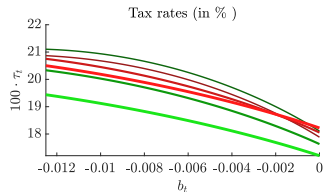
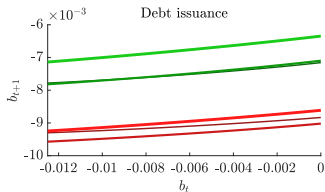
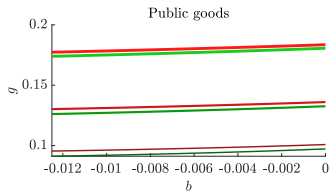
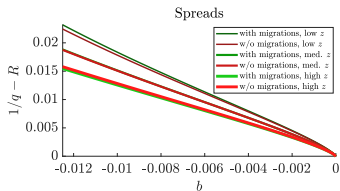
Calibration (for $T = 30$ years)

Parameter	Description	Value	Calibration target
σ	Survival rate	0.30	Old age dependency ratio
α	Output elasticity of capital	0.33	Standard value in the literature
R	Riskless interest rate	3.24	Annual real interest rate of 4%
ρ_T	Persistence of the AR(1) process	0.61	Country-level productivity process
$\sigma_{\epsilon, T}$	Std. error of the AR(1) process	0.08	Country-level productivity process
χ_0	Parameter of default penalty	0.05	Mean debt to GDP ratio of 72%
χ_1	Parameter of default penalty	2.35	Mean spread over riskless rate of 1.2%
θ^o	Preferences for public goods	1.00	Public goods for the elderly to GDP of 12%
ψ_1	Parameter of matching technology	0.20	Intra-EU migrations
ψ_2	Parameter of matching technology	2.57	Intra-EU migrations
ϕ	Parameter of matching technology	1.09	Intra-EU migrations

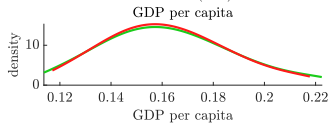
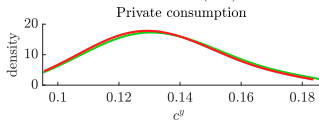
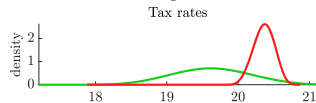
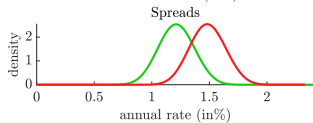
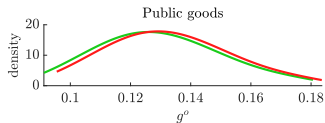
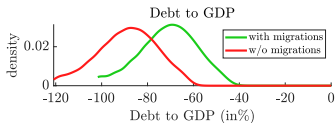
Calibration: matching process



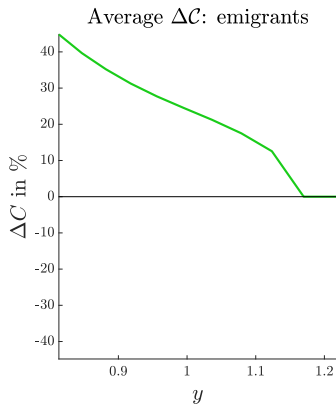
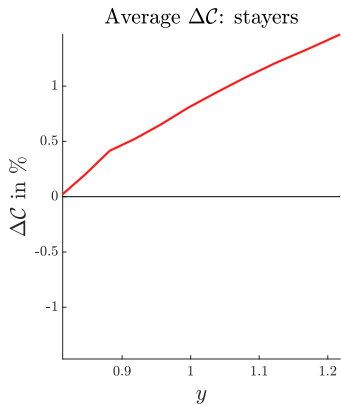
Results: optimal policies at the country level



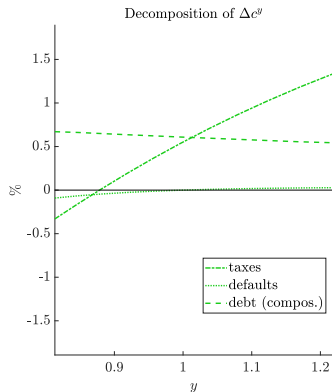
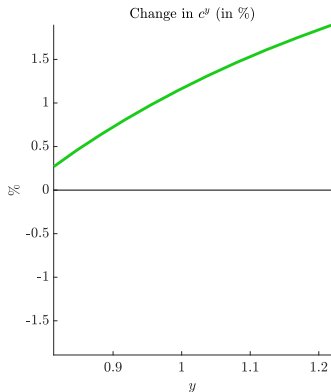
Results: distributions of countries over variables and policies



Results: welfare



Results: decomposition of c^y



- Optimal government policies and migrations
 - less public goods for the old
 - lower debt levels
 - amplification of defaults
- Labor mobility and economic union
 - important general equilibrium effects of fiscal discipline
 - lower average debt - lower spreads
 - + lower taxes - higher private consumption
 - welfare gains even for less productive economies

Thank you for your
attention!

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- Labor mobility and sovereign default: Alessandria et al. [2019]

Formulas for E and I

Country-level number of emigrants:

$$E(n^o, U^y, \Omega) = n^o \cdot \left[\sum_{\hat{B}, \hat{y}, \hat{n}^o} \mathbb{P}_{\Phi} \left(U^y \left(\hat{n}^o, \hat{B}, \hat{y} \right) \mid \Omega \right) \right. \\ \times \frac{\mu \left(\hat{n}^o, \hat{B}, \hat{y} \right) \cdot \hat{n}^o}{\sum_{\tilde{B}, \tilde{y}, \tilde{n}^o} \mathbb{I} \{ U^y \left(\tilde{n}^o, \tilde{B}, \tilde{y} \right) = U^y \left(\hat{n}^o, \hat{B}, \hat{y} \right) \} \cdot \mu \left(\tilde{n}^o, \tilde{B}, \tilde{y} \right) \cdot \tilde{n}^o} \\ \left. \times \Psi \left(\frac{\mathcal{C} \left(U^y \left(\hat{n}^o, \hat{B}, \hat{y} \right) \right) - \mathcal{C} \left(U^y \left(n^o, B, y \right) \right)}{\mathcal{C} \left(U^y \left(n^o, B, y \right) \right)} \right) \right].$$

Immigrants arriving to the analyzed economy:

$$I(n^o, U^y, \Omega) = \sum_{\hat{B}, \hat{y}, \hat{n}^o} \left[\mu \left(\hat{n}^o, \hat{B}, \hat{y} \right) \cdot \hat{n}^o \cdot \mathbb{P}_{\Phi} \left(U^y \mid \Omega \right) \right]$$

$$\frac{1 \cdot n^o}{\sum_{\tilde{B}, \tilde{y}, \tilde{n}^o} \mathbb{I}_{\{U^y(\tilde{n}^o, \tilde{B}, \tilde{y}) = U^y\}} \cdot \mu(\tilde{n}^o, \tilde{B}, \tilde{y}) \cdot \tilde{n}^o} \Psi \left(\frac{\mathcal{C}(U^y) - \mathcal{C}(U^y(\hat{n}^o, \hat{B}, \hat{y}))}{\mathcal{C}(U^y(\hat{n}^o, \hat{B}, \hat{y}))} \right) \Bigg].$$

Probability $\mathbb{P}_\Phi(\hat{U}^y|\Omega)$ of drawing opportunity \hat{U}^y from distribution characterized with c.d.f. $\Phi \circ F$:

$$\mathbb{P}_\Phi(\hat{U}^y|\Omega) = \lim_{\epsilon \rightarrow 0} \left\{ \Phi \circ F(\hat{U}^y + \epsilon) - \Phi \circ F(\hat{U}^y - \epsilon) \right\}$$

Intermediary: maximization problem i

Similar to Chatterjee et al. [2007] (financial intermediaries sell the amount \bar{K}_{t+1} of capital, choose the number A of type (b', y) sovereign loan/deposit contracts at price q and A^P of private loan/deposit contracts signed with households populating a country indexed with (b, y) traded at price q^P , to maximize the discounted sum of profits):

$$\sum_{t=0}^{+\infty} R^{-t} \cdot \Pi_t$$

where:

$$\begin{aligned} \Pi_t = & (1 - \delta + R^f) \cdot \bar{K}_t - \bar{K}_{t+1} \\ + & \sum_{b_{t+1}, y_t} q(b_{t+1}, y_t) \cdot A(b_{t+1}, y_t) \cdot b_{t+1} - \sum_{b_t, y_{t-1}} (1 - d(b_t, y_{t-1})) \cdot A(b_t, y_{t-1}) \cdot b_t \end{aligned}$$

Intermediary: maximization problem ii

$$+ \sum_{b_t, y_t} A^P(b_t, y_t) \cdot a_{t+1}(b_t, y_t) - \sum_{b_{t-1}, y_{t-1}} \sigma \cdot R^h \cdot A^P(b_{t-1}, y_{t-1}) \cdot a_t(b_{t-1}, y_{t-1}) .$$

◀ back

Markov Perfect Equilibrium i

Definition: A Stationary Markov Perfect Competitive Equilibrium (SMPCE) consists of prices R^f, R^h , debt contracts $q(b', y)$, wages w , household policies c^y, c^o, a' , government policies τ, d, b', g , choices of financial intermediaries A, A^P, \bar{K}' , distribution μ^ and function η , such that:*

- 1. Policies c^y, c^o, a' solve household problem given τ, g', R^h and w ,*
- 2. Policies τ, d, b', g solve government's problem given Γ, w, q, η ,*
- 3. First order conditions associated with financial intermediaries problem hold*
- 4. Markov Perfect Equilibrium condition holds*
- 5. Consistency conditions hold*
- 6. Pareto weights satisfy $\alpha^y = \eta$ and $\alpha^o = \sigma$*

Law of motion of countries across states:

$$\mu'(n^{o'}, b', y') = \sum_{n^o, b, y} \left[\pi(y'|y) \cdot \mathbb{I}_{\{\eta(U^y(b, y), \Omega) \cdot n^o = n^{o'}\}} \right. \\ \left. \cdot \mathbb{I}_{\{b'(b, y) = b'\}} \cdot \mu(n^o, b, y) \right]$$

Markov Perfect Equilibrium condition:

$$\forall_{b, y} g(b, y) = \Gamma(b, y)$$

Results: distributions of countries over variables and policies

	Migration	No migration
Union output	0.3265	0.3235
Mean debt-to-GDP ratio	71.2%	89%
Std.dev. of debt-to-GDP	12.5%	12.9%
Mean spread over R	1.21%	1.43%