

Forward Guidance: Communication, Commitment, or Both?

Marco Bassetto

Federal Reserve Bank of Chicago, and IFS

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Distinction between:

- “Odyssean” forward guidance: meant as a form of commitment
- “Delphic” forward guidance: central bank has superior information, reveals it to the public

- Forward guidance: a set of statements about *likely future policy* that:
 - does not **directly** constrain central bank actions
 - does not **directly** change future decision process
 - does not **directly** affect payoffs

Forward Guidance as Cheap Talk

- Forward guidance: a set of statements about *likely future policy* that:
 - does not **directly** constrain central bank actions
 - does not **directly** change future decision process
 - does not **directly** affect payoffs
- Forward guidance is cheap talk (in the technical sense)

Goal of this Project

- When does forward guidance work?
- How does it work?
- What does it communicate?

Necessary Ingredients for a Model

- A monetary game
- Expectations about future policy must be important
- Must study repeated interaction (the role of credibility, reputation, “embarrassment”)
- Must be simple enough to be transparent

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- Expectations about future policy must be important
- Must study repeated interaction (the role of credibility, reputation, “embarrassment”)
- Must be simple enough to be transparent
- Will work with (a variant of) the Barro-Gordon model
- Insights carry over to standard DSGE models...
- ... with no need to deal with complications (neo-Fisherian solutions, fiscal theory,...)

The Model: Shocks

- Potential output \hat{y}_t
- Inflation target π_t^*
- Sunspot (public randomization device) s_t (only for technical reasons)

- At time 0: Nature draws $\{\hat{y}_t, \pi_t^*, s_t\}_{t=0}^{\infty}$
- At time t :
 - Government, private sector receive information: filtration \mathcal{G}_t and \mathcal{F}_t
 - Government may send messages $M_t \in \mathcal{M}$
 - Households set their expectations y_t^e, π_t^e (either no heterogeneity or aggregation through linearity).
 - Government sets inflation π_t
 - Output realized
 - Households observe gov't information

The Phillips curve

$$y_t = \theta \hat{y}_t + (1 - \theta)y_t^e + \lambda(\pi_t - \pi_t^e).$$

- \hat{y}_t : potential output
- In Barro-Gordon, $\theta = 1$
- $\theta < 1$ allows imperfect information about \hat{y}_t to matter

$$E \sum_{t=0}^{\infty} \beta^t \left\{ (y_t - \hat{y}_t - k)^2 + \alpha [\pi_t - \pi_t^* - f(\hat{y}_t)]^2 \right\}$$

- As in Barro-Gordon, k distortion implies gov't wants to overstimulate
- Allow for inflation-output interaction through $f(\hat{y}_t)$
- $f(\hat{y}_t) \neq 0$ will mean that optimal ex ante inflation is not constant wrt output

Gov't loss function, household behavior

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- Households set

$$y_t^e = E[y_t | \mathcal{F}_t, m_t]$$

$$\pi_t^e = E[\pi_t | \mathcal{F}_t, m_t]$$

▶ [Go to definition of strategies, equilibrium](#)

Equilibrium set

- Big in general (trigger strategies, tit-for-tat, repeated Nash, multiple possible partitions,...)
- Can be computed using Abreu-Pierce-Stacchetti methods.

- Study a sequence of economies
- In the first one, messages are redundant
- In the second one, they have an important role, but they are not about policy
- Finally, in the last two forward guidance emerges

A Simple Model without Private Information

- Assume $\mathcal{F}_t = \mathcal{G}_t$
- Government has no information advantage over the private sector

An Equivalence Theorem

- Compare a case in which $\mathcal{M} = \emptyset$ (no messages) and one where $\mathcal{M} \neq \emptyset$
- In both games, equilibrium strategies induce a prob. distr. over equilibrium sequences for $\{\pi_s, y_s\}_{s=0}^{\infty}$.
- The set of prob. distr. over equilibrium sequences is the same in the two games
- Forward guidance is a redundant instrument

- Public announcement is supposed to cause “embarrassment” if policy deviates (Odyssean forward guidance)
- But everybody knows what the right action is
- Trigger based directly on action
- No need to speak, but just to *act!*

▶ Go to example

Adding private information about the Economy

- Assume gov't observes same info as households + advance signal \tilde{y}_t
- Assume $f(\hat{y}_t) \equiv 0$ (that is, optimal policy π_t^* is independent of output)

▶ What if $f(\hat{y}_t) \neq 0$?

Optimal Policy under Commitment (before observing \tilde{y}_0)

- Reveal signal truthfully: $m_t = \tilde{y}_t$;
- Set inflation to π_t^* .
- Note: announcement strictly improves welfare (cheap talk is essential)

Result under discretion

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- When β close to 1 or gov't info sufficiently more precise than private, sending messages expands set of equilibrium payoffs
- When β close to 1 and $\bar{\pi}$ (maximal possible inflation) sufficiently high, sending messages only expands towards high payoffs

▶ More details

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- CB reporting information about underlying economy, not its policy
- **In the example**, when best=commitment, policy (inflation) unaffected by information
- Reporting policy would not substitute for direct report of information

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- Symmetric info about \hat{y}_t ; for simplicity, assume $f(\hat{y}_t) \equiv 0$
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- Symmetric info about \hat{y}_t ; for simplicity, assume $f(\hat{y}_t) \equiv 0$
- Asy info about π_t^*
- **Given policy**, private sector has all the info needed to take decisions
- Asy. info only relevant for forecasting CB policy

Optimal Policy under Commitment (best equilibrium outcome for large β)

- Announce truthfully $m_t = \pi_t^*$;
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- Forward guidance is directly about CB policy
- With β sufficiently close to 1 or target sufficiently dispersed, cheap talk valuable under discretion, expands set of eq. payoffs

Delphic forward guidance: asy info over beliefs

- Assume symmetric info about π_t^*
- Households observe \hat{y}_t perfectly (only need better than gov't)
- Gov't observes imperfect signal \tilde{y}_t

Optimal Policy under Commitment (best equilibrium outcome for large β)

- Two options:
 - Announce truthfully \tilde{y}_t
 - Announce $\pi_t^* + E[f(\hat{y}_t)|\mathcal{G}_t]$
- Set inflation to $\pi_t^* + E[f(\hat{y}_t)|\mathcal{G}_t]$

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What Does this Suggest about Forward Guidance in Practice?

- Can communicate insights into decision process
- Can signal agreement, disagreement among policymakers
- Can signal models policymakers believe in (Krugman-Woodford-Eggertsson)

- Forward guidance useful when CB has superior information about its preferences and beliefs
- Credibility and forward guidance interact, but are not the same

Histories and Strategies

- A (public) history at the message stage is $h^t := \{m_s, \pi_s\}_{s=0}^{t-1}$.
- A (public) history at the expectations-setting stage
 $h^{et} := (\{m_s, \pi_s\}_{s=0}^{t-1}, m_t)$
- Set of histories: H^t, H^{et} (use Borel σ -algebra)
- Underlying state of nature: ω
- A CB strategy is a \mathcal{G}_t -measurable mapping σ^g from (Ω, H^t) into a distribution over \mathcal{M} , and from (Ω, H^{et}) into a distribution over $[\underline{\pi}, \bar{\pi}]$
- A (symmetric) household strategy is a \mathcal{F}_t -measurable mapping σ^p from (Ω, H^{et}) to $[\underline{\pi}, \bar{\pi}] \times [y^\ell, y^h]$

From strategies to outcomes

- Given a pair (σ^G, σ^P) ...
- ... obtain a probability distribution over histories (ω, H^∞)

Equilibrium (using one-deviation principle)

- A strategy profile (σ^g, σ^p) such that:
- Given any (ω, h^t) and given that future play will occur according to σ^g, σ^p , any message in the support of $\sigma^g(\omega, h^t)$ is optimal for gov't
- Given any (ω, h^{et}) and given that future play will occur according to σ^g, σ^p , any inflation rate in the support of $\sigma^g(\omega, h^{et})$ is optimal for gov't
- Given any (ω, h^{et}) and σ^g ,

$$y_t^e = E[y_t | \mathcal{F}_t, m_t; \sigma^g]$$

$$\pi_t^e = E[\pi_t | \mathcal{F}_t, m_t; \sigma^g]$$

▶ Back to equilibrium set

An example

- Set $\lambda = 40$, $\hat{y} = 0.01$, $\beta = 0.96$, $\pi^* = 0.02$, $\alpha = 1$
- One equilibrium (trigger strategy):
- CB offers “forward guidance” that inflation will be 2%;
- Private sector believes announcement if and only if previous announcements were truthful (and announced value less than 43%)
- Otherwise, private sector disregards announcement, expects repeated Nash, 43%
- CB sets π_t equal to announcement (2%) if truthful in the past (and announcement less than 43%), to 43% otherwise

Equilibrium without Cheap Talk

- Private sector expects 2% inflation, unless different inflation rate occurred in the past
- Otherwise, private sector expects 43%
- CB sets π_t to 2% if it never deviated from 2% in the past, to 43% otherwise

▶ Back to no private information

- Folk theorem (for β), standard cheap talk (for y^ℓ)
- Why no expansion towards low payoffs? Announcements...
 - Improve best payoff, allow for better continuation promises after punishment stage of worst
 - Tighten incentive-compatibility constraint of worst, harder to punish gov't (may both misreport and choose different inflation)

- Folk theorem (for β), standard cheap talk (for y^ℓ)
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 - Tighten incentive-compatibility constraint of worst, harder to punish gov't (may both misreport and choose different inflation)
 - For high $\beta, \bar{\pi}$, continuation of worst is not best, first element not present

▶ [Back to Delphic announcements](#)

Announcements when \hat{y}_t affects optimal inflation

- Under commitment, $\pi_t = \pi_t^* + E[f(\hat{y}_t)|\mathcal{G}_t]$
- Announcement about π_t would reveal information
- Still imperfect, households would want to know signal
- ... also more natural, when people really care about state

▶ [Back to Delphic announcements](#)