

***Keynesian Micromanagement* by Ghassibe and Zanetti: discussion by Paweł Kopiec (NBP)**

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Q: What is the optimal response of fiscal policy to large and asymmetric shocks in a multi-sector economy?

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Keynesian Micromanagement by Ghassibe and Zanetti:

- Model:
 - search frictions
 - multiple sectors
- Results:
 - optimal fiscal policy
 - search frictions \sim TFP changes

Optimal sector-specific spending in Ghassibe and Zanetti

- Government maximizes:

$$\max_{\{G_i\}_{i=1}^N} \mathcal{U} [D_1 (C_1, G_1), \dots, D_N (C_N, G_N)]$$

- Subject to:

$$\forall_{i \in \{1, \dots, N\}} (1 + \gamma_i (x_i)) \cdot \left(C_i + G_i + \sum_{j=1}^N Z_{ji} \right) = f_i (x_i) \cdot K_i$$

$$\sum_{i=1}^N L_i = \bar{L}, M = \bar{M}, + \text{optimality conditions}$$

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My assumptions

- Competitive equilibrium (CE) given G
- Special case:
 - $\sigma = 1$ (log-log utility)
 - $\bar{L} = 1$ (unit mass of workers)
 - $N = 1$ (one sector)
 - $r = 1$ (fixprice equilibrium as in Michailat and Saez [2015])
 - $\psi^h = 1$ (matching standardization)
 - $\theta = 1$ (Cobb-Douglas production function)
 - $\delta = 0$ (no taste for public goods)

- Households:

$$\max_{C, M} \log C + \mu \cdot \log M$$

$$P \cdot (1 + \gamma(x)) \cdot C + M \leq W \cdot \bar{L} + \bar{M} + \Pi - T$$

- Firms:

$$\Pi = \max_{L, Z} \left\{ P \cdot f(x) \cdot L^{1-\alpha} \cdot Z^\alpha - W \cdot L - P \cdot (1 + \gamma(x)) \cdot Z \right\}$$

- Government:

$$P \cdot (1 + \gamma(x)) \cdot G = T$$

- Price-setting, wage-setting, market clearing - labor/numeraire:

$$P = \text{const.}, x, W - \text{flexible}, L = \bar{L}, M = \bar{M}$$

- Market clearing - manufactured goods:

$$(1 + \gamma(x)) \cdot (C + G) = \underbrace{f(x) \cdot L^{1-\alpha} \cdot Z^\alpha - (1 + \gamma(x)) \cdot Z}_{\equiv Y}$$

CE given G : a characterization

CE under **optimal policy** $G = 0$:

$$\underbrace{\frac{\bar{M}}{\mu \cdot P}}_{=(1+\gamma(x)) \cdot C} = \underbrace{\frac{f(x)^{\frac{1}{1-\alpha}}}{(1+\gamma(x))^{\frac{\alpha}{1-\alpha}}} \cdot \left(\alpha^{\frac{\alpha}{1-\alpha}} - \alpha^{\frac{1}{1-\alpha}} \right)}_{=Y(x)} \quad (1)$$

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Proposition. $Y(x)$ is a single-peaked curve with $Y'(x^P) = 0$ where $x^P \equiv \left[\frac{\alpha \cdot \rho \cdot \eta}{1-\eta} + \rho \right]^{-\frac{1}{\eta}}$. If $G = 0$ (optimal policy) then:

- If $\frac{\bar{M}}{\mu \cdot P} > Y(x^P)$ then (1) has **no** solutions.
- If $\frac{\bar{M}}{\mu \cdot P} = Y(x^P)$ then (1) has **a unique** solution,
- If $\frac{\bar{M}}{\mu \cdot P} \in (0, Y(x^P))$ then (1) has **two** solutions,

CE given G : a characterization

CE under **optimal policy** $G = 0$:

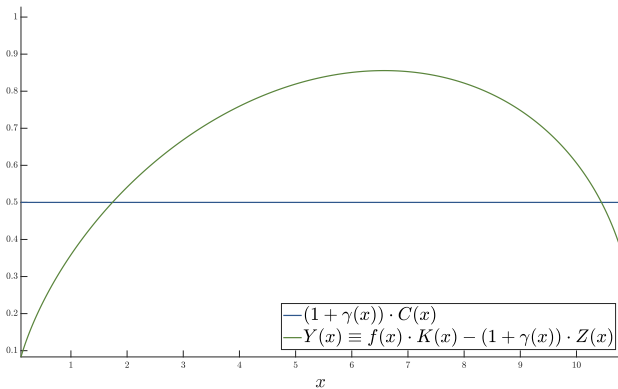
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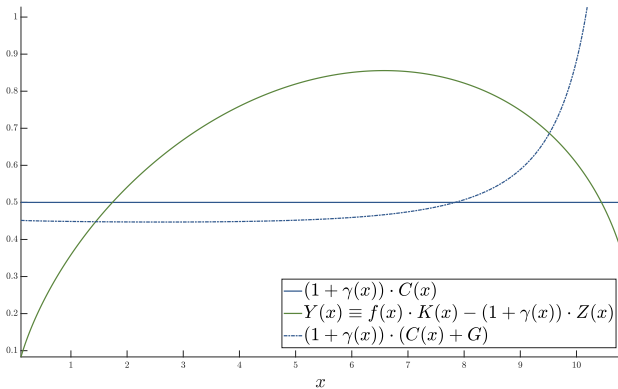
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Proof: [▶ details](#)

CE given G : graphical illustration when $\delta > 0, G = 0$



CE given G : graphical illustration when $\delta > 0, G > 0$



Three questions and three answers

- **Q1:** Can the government guarantee that the preferred equilibrium materializes?
- **A1:** Not really, after choosing G the economy may suffer from a coordination failure.
- **Q2:** Which of the two equilibria is preferred by the government?
- **A2:** The 'low x ' CE is strictly preferred (at least in the neighborhood of $G = 0$).
- **Q3:** Are the stimulus effects in the 'low x ' equilibrium realistic?
- **A3:** It may occur that $\delta > 0$ leads to $\frac{dY}{dG} < 0$...

More details on A1-A3: [▶ details](#)

- Networks in macro:
 - theoretical: Acemoglu et al. [2012], Taschereau-Dumouchel [2017], Baqaee [2018], Baqaee and Farhi [2019], Baqaee and Farhi [2020]
 - empirical: Cox et al. [2020], Ghassibe [2021], Barattieri et al. [2023]
- Frictional product market:
 - theory: Michaillat and Saez [2015]
 - TFP/demand: Storesletten et al. [2011]
- Optimal fiscal policy with:
 - search frictions: Michaillat and Saez [2019]
 - search frictions + **multiple sectors**: Ghassibe and Zanetti [2023]
 - search frictions + **default risk**: Kiiashko and Kopiec [2023]

Thank you for your
attention!

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Let us first derive equation (1). To this end, notice that the household's first order condition is:

$$(1 + \gamma(x)) \cdot C = \frac{M}{P \cdot \mu}. \quad (2)$$

when $\delta = 0$. Firm's optimality conditions are:

$$P \cdot f(x) \cdot (1 - \alpha) \cdot L^{-\alpha} \cdot Z^{\alpha} = W \quad (3)$$

$$P \cdot f(x) \cdot \alpha \cdot L^{1-\alpha} \cdot Z^{\alpha-1} = P \cdot (1 + \gamma(x)) \quad (4)$$

Analogously to Michailat and Saez [2015], combining the market clearing for numeraire good with (2) yields:

$$(1 + \gamma(x)) \cdot C = \frac{\bar{M}}{P \cdot \mu}. \quad (5)$$

Combining (4) with the labor market clearing condition (i.e., $L = \bar{L} = 1$) gives:

$$Z = \left[\frac{\alpha \cdot f(x)}{1 + \gamma(x)} \right]^{\frac{1}{1-\alpha}}. \quad (6)$$

Now, plugging (5) and (6) into the consumption goods market clearing condition yields:

$$\frac{\bar{M}}{P \cdot \mu} + (1 + \gamma(x)) \cdot G = f(x) \cdot \left[\frac{\alpha \cdot f(x)}{1 + \gamma(x)} \right]^{\frac{\alpha}{1-\alpha}} - (1 + \gamma(x)) \cdot \left[\frac{\alpha \cdot f(x)}{1 + \gamma(x)} \right]^{\frac{1}{1-\alpha}}$$

which, after reformulation, gives:

$$\frac{\bar{M}}{\mu \cdot P} + G \cdot (1 + \gamma(x)) = \frac{f(x)^{\frac{1}{1-\alpha}}}{(1 + \gamma(x))^{\frac{\alpha}{1-\alpha}}} \cdot \left(\alpha^{\frac{\alpha}{1-\alpha}} - \alpha^{\frac{1}{1-\alpha}} \right) \quad (7)$$

Proof iii

which is equation (1). Notice that x pins down the equilibrium value(s) of x , which can be then used for computing the remaining equilibrium objects (Z from (6) given x , W from (3) given Z and $L = \bar{L} = 1$, C from (5), etc.). Let us turn to the proof of the Proposition. Note that we consider a special case when $G = 0$ (as explained later, this corresponds to the optimal fiscal policy in the economy when $\delta = 0$). All this implies that (7) becomes:

$$\frac{\bar{M}}{\mu \cdot P} = \frac{f(x)^{\frac{1}{1-\alpha}}}{(1 + \gamma(x))^{\frac{\alpha}{1-\alpha}}} \cdot \left(\alpha^{\frac{\alpha}{1-\alpha}} - \alpha^{\frac{1}{1-\alpha}} \right). \quad (8)$$

The LHS of (8) is a constant. The RHS of (8) is a function of x and is denoted by $Y(x)$. Let us investigate the monotonicity of $Y(x)$. To this, end, let us compute the derivative:

$$Y'(x) = \frac{d}{dx} \left(\frac{f(x)^{\frac{1}{1-\alpha}}}{(1 + \gamma(x))^{\frac{\alpha}{1-\alpha}}} \cdot \left(\alpha^{\frac{\alpha}{1-\alpha}} - \alpha^{\frac{1}{1-\alpha}} \right) \right)$$

$$\begin{aligned}
 &= \frac{\left(\alpha^{\frac{\alpha}{1-\alpha}} - \alpha^{\frac{1}{1-\alpha}}\right)}{\left((1 + \gamma(x))^{\frac{\alpha}{1-\alpha}}\right)^2} \cdot \left(\frac{1}{1-\alpha} \cdot f(x)^{\frac{1}{1-\alpha}-1} \cdot f'(x) \cdot (1 + \gamma(x))^{\frac{\alpha}{1-\alpha}}\right. \\
 &\quad \left. - f(x)^{\frac{1}{1-\alpha}} \cdot \frac{\alpha}{1-\alpha} \cdot (1 + \gamma(x))^{\frac{\alpha}{1-\alpha}-1} \cdot \gamma'(x)\right) \\
 &= \frac{\left(\alpha^{\frac{\alpha}{1-\alpha}} - \alpha^{\frac{1}{1-\alpha}}\right)}{\left((1 + \gamma(x))^{\frac{\alpha}{1-\alpha}}\right)^2} \cdot \frac{f(x)^{\frac{1}{1-\alpha}} \cdot (1 + \gamma(x))^{\frac{\alpha}{1-\alpha}}}{1-\alpha} \\
 &\quad \cdot \left[\frac{f'(x)}{f(x)} - \alpha \cdot \frac{\gamma'(x)}{1 + \gamma(x)}\right].
 \end{aligned}$$

It is clear that the term outside the square bracket is positive because $\alpha \in (0, 1)$, $f(x) > 0$, $\gamma(x) > 0$ (the last inequality follows, because as argued by Michailat and Saez [2015], the equilibrium in the model is well-defined if $q(x) > \rho$, i.e., for $x \in (0, \bar{x})$ where

$q(\bar{x}) = \rho$. All this implies that the sign of $Y'(x)$ is equal to the sign of the following term:

$$\begin{aligned}
 & \frac{f'(x)}{f(x)} - \alpha \cdot \frac{\gamma'(x)}{1 + \gamma(x)} \\
 &= \frac{f'(x)}{f(x)} - \alpha \cdot \frac{\left(-\frac{\rho \cdot q'(x)}{(q(x) - \rho)^2}\right)}{1 + \frac{\rho}{q(x) - \rho}} \\
 &= \frac{f'(x)}{f(x)} + \alpha \cdot \rho \cdot \frac{q'(x)}{q(x) \cdot (q(x) - \rho)} \\
 &= \frac{(1 - \eta) \cdot x^{-\eta}}{x^{1-\eta}} + \alpha \cdot \rho \cdot \frac{-\eta \cdot x^{-\eta-1}}{x^{-\eta} \cdot (x^{-\eta} - \rho)} \\
 &= \frac{1}{x} \cdot \left(1 - \eta - \frac{\alpha \cdot \rho \cdot \eta}{x^{-\eta} - \rho}\right)
 \end{aligned}$$

given that $\frac{1}{x}$ is always strictly positive for $x \in (0, \bar{x})$, the sign of $Y'(x)$ is the same as the sign of:

$$1 - \eta - \frac{\alpha \cdot \rho \cdot \eta}{x^{-\eta} - \rho}. \quad (9)$$

Note that term (9) converges to a positive value of $1 - \eta$ as $x \rightarrow 0$ and it converges to $-\infty$ as $x \rightarrow \bar{x}$ (observe that $q(x) = x^{-\eta} \rightarrow \rho$ when $x \rightarrow \bar{x}$). Moreover, it is obvious that (9) is a strictly decreasing function of x for $x \in (0, \bar{x})$. All this implies that, (9) attains the level of zero only once and that $Y(x)$ achieves maximum at $x = x^P$ that satisfies:

$$1 - \eta - \frac{\alpha \cdot \rho \cdot \eta}{x^{-\eta} - \rho} = 0$$
$$\Leftrightarrow x = x^P = \left[\frac{\alpha \cdot \rho \cdot \eta}{1 - \eta} + \rho \right]^{-\frac{1}{\eta}}$$

and that $Y(x)$ is a single-peaked function. Now, given that the LHS of (8) is constant and that $Y(x)$ is single-peaked with the maximum equal to $Y(x^P)$, (8) has two solutions for $\frac{\bar{M}}{\mu \cdot P} \in (0, Y(x^P))$, one solution for $\frac{\bar{M}}{\mu \cdot P} = Y(x^P)$ and no solutions for $\frac{\bar{M}}{\mu \cdot P} > Y(x^P)$. To see that $G = 0$ is indeed optimal (more precisely: it guarantees that the best possible outcome is among the resulting equilibria), consider the only interesting case when $\frac{\bar{M}}{\mu \cdot P} \in (0, Y(x^P))$ (notice that if $\frac{\bar{M}}{\mu \cdot P} \geq Y(x^P)$ then $G > 0$ implies that there are no equilibria because $1 + \gamma(x) > 0$). Suppose that, by contradiction, $G > 0$: this implies that curve $(1 + \gamma(x)) \cdot G$ is added to $\frac{\bar{M}}{\mu \cdot P}$ in condition (7) and both resulting equilibria (if G is not too large) feature higher x than the equilibrium characterized with 'low x ' when $G = 0$ (it is useful to use the properties of Y to see this fact) which coupled with (2) implies lower consumption and lower welfare in those equilibria when $G > 0$. Q.E.D.

◀ back

A1: The convention in the model is as follows: government sets G and then the market forces shape the ultimate outcome/allocation. The problem is that there can be (as argued in my discussion) two equally possible outcomes achieved by those forces (for a given value of G). The question is whether the government can fix things by making agents believe that the preferred equilibrium (e.g. the 'low x ' one) is the one that will actually materialize. This certainly requires some additional assumptions on the government's impact on agents' expectations that would allow for avoiding the coordination failure.

A2: Note that, when $G = 0$, $Y(x)$ is equal in both equilibria. At the same time, the amount of resources spent on wasteful search activities is larger in the 'high x ' equilibrium because $\gamma(x)$ is an increasing function. Therefore, the 'high x ' equilibrium should not be preferred by the government because the total amount resources that can be spent on private consumption C and government spending G is strictly lower than in the 'low x ' equilibrium.

A3: The problem with $\frac{dY}{dG} < 0$ is that there is a broad consensus that fiscal multipliers are positive. $\frac{dY}{dG} < 0$ may occur when $\delta > 0$ because C and G may be regarded by households as substitutes and thus higher G makes them consume less C . Note also that when $\delta = 0$ the multipliers are always positive.

◀ back